

**Обнаружение дополнительного механизма
электролюминесценции в двухфазных детекторах темной
материи: тормозное излучение электронов на атомах**

**Revealing additional mechanism of proportional
electroluminescence in two-phase dark matter detectors:
neutral bremsstrahlung**

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**Экспериментальный семинар ИЯФ
23/03/2018**

Group of cryogenic and avalanche detectors for rare-event experiments

Group of Cryogenic and Avalanche Detectors is combined from Lab 3-3 (BINP) and Lab of Cosmology and Elementary Particles (NSU)

The group is operated in the frame of BINP and NSU research programs:

A. Bondar (head of Lab 3-3), A. Buzulutskov (leader of group), A. Dolgov (head of LCECh), A. Chegodaev, E. Frolov, V. Nosov, V. Oleynikov, T. Shakirova, L. Shekhtman, E. Shemyakina, R. Snopkov, A. Sokolov

We collaborate with S. Polosatkin on neutron scattering system and with V. Parkhomchuk and A. Petrozhitski on low-pressure TPC for ion ID.

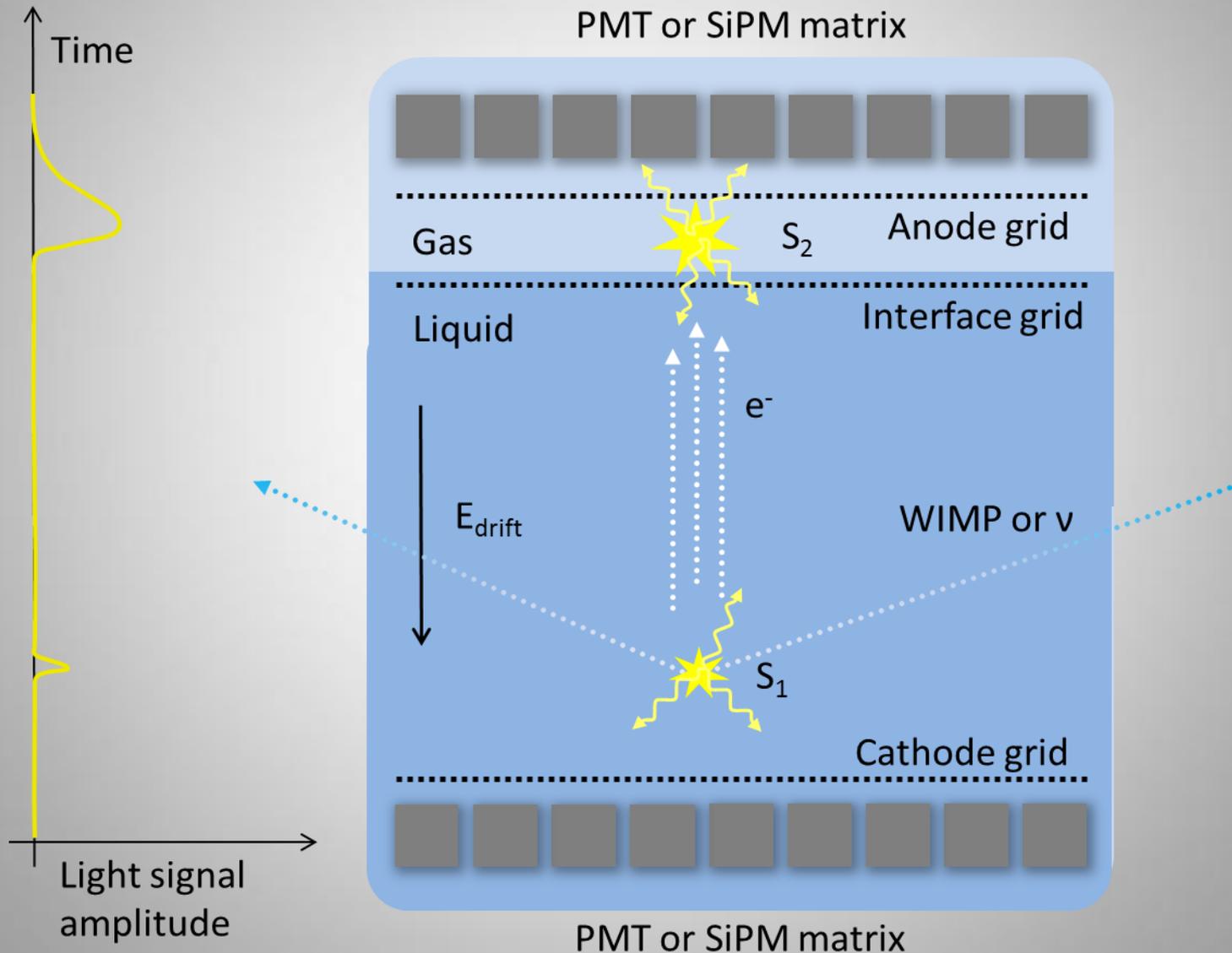
We are members of DarkSide-20k collaboration

Outline

1. The problem of proportional electroluminescence (EL) in two-phase Ar
2. Neutral bremsstrahlung (NBrS): history and theory
3. Experimental setup
4. EL yields: experiment vs theory
5. Applications of NBrS EL
6. Conclusions

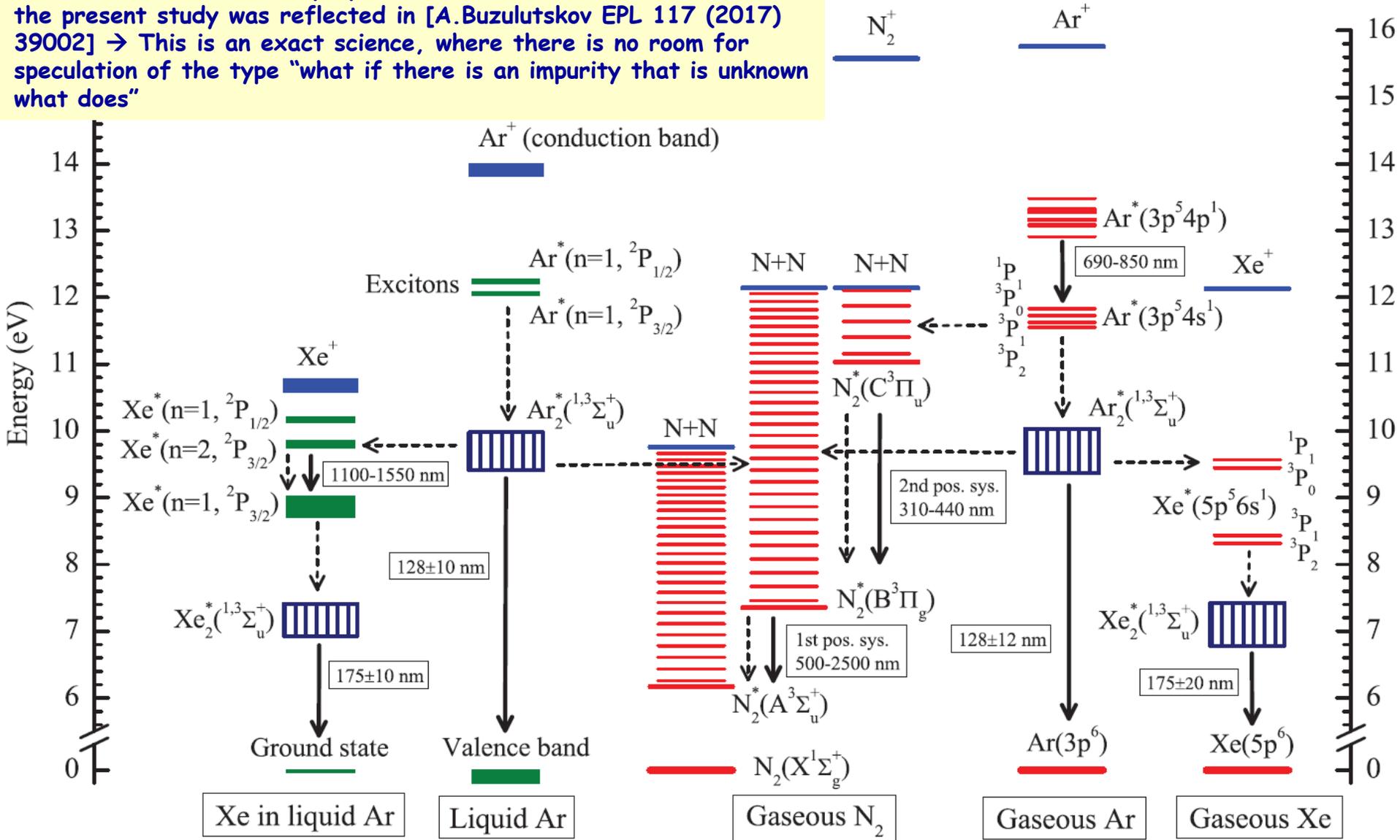
Section 1. The problem of proportional EL in two-phase Ar

Two-phase dark matter detectors: principles of operation



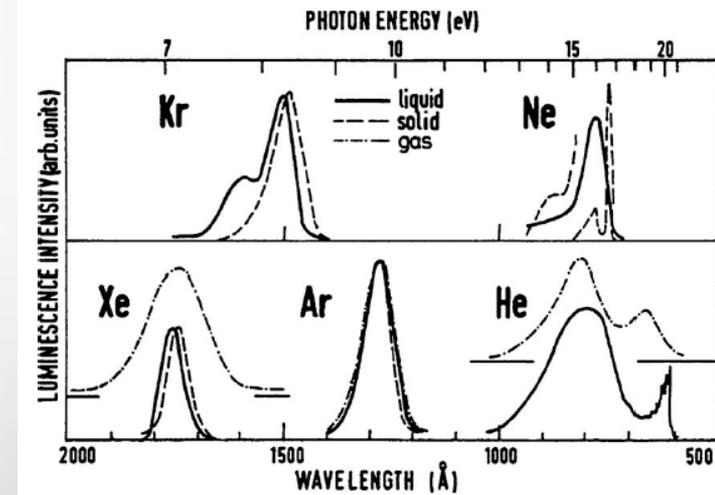
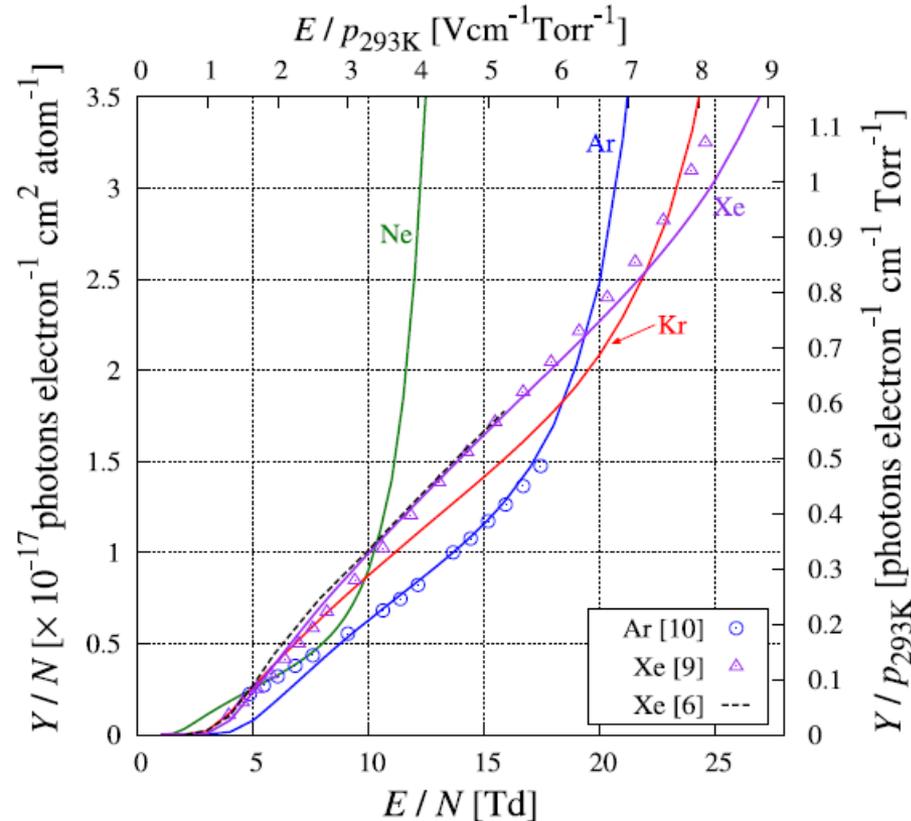
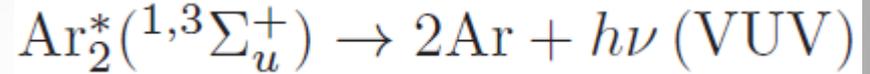
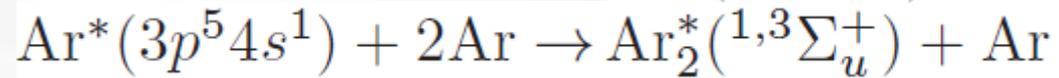
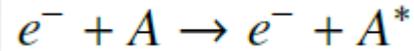
Photon emission and collisional processes in gaseous and liquid Ar doped with Xe and N₂

All that was known about proportional electroluminescence before the present study was reflected in [A.Buzulutskov EPL 117 (2017) 39002] → This is an exact science, where there is no room for speculation of the type "what if there is an impurity that is unknown what does"



Proportional EL in GAr: ordinary EL - strong emission in VUV

Strong ordinary EL in the VUV (128 nm) due to excimers,
via $\text{Ar}^*(3p^5 4s^1)$ excited states, at >4 Td:

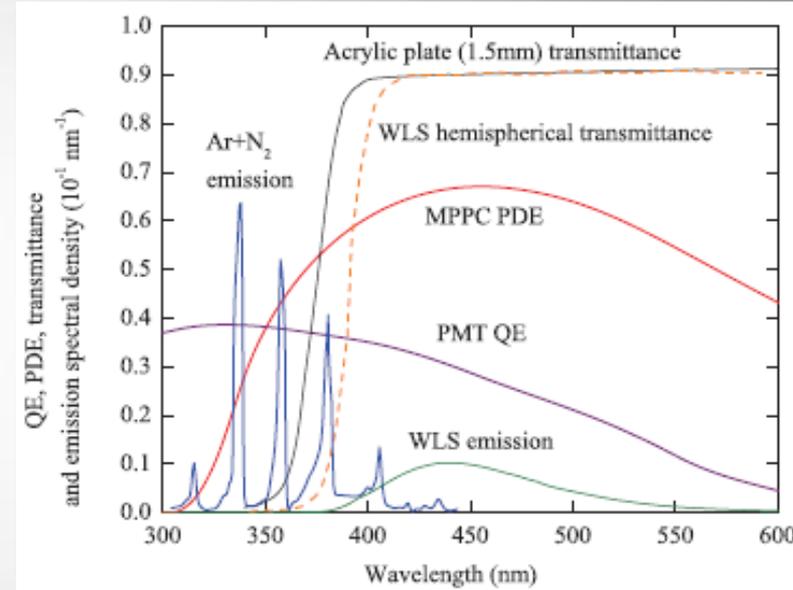
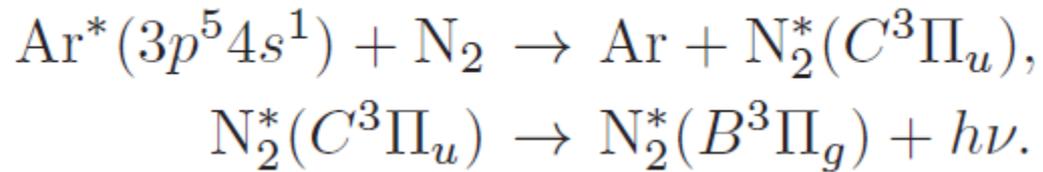


Satisfactory agreement between
the microscopic theory and
experiment

Proportional EL in GAr:

EL in presence of N₂ (~1%) - strong emission in near UV, competing to ordinary EL in the VUV

In the presence of N₂ dopant, EL in the near UV due to excitation transfer from Ar to N₂ and N₂ emission of 2nd Positive System:



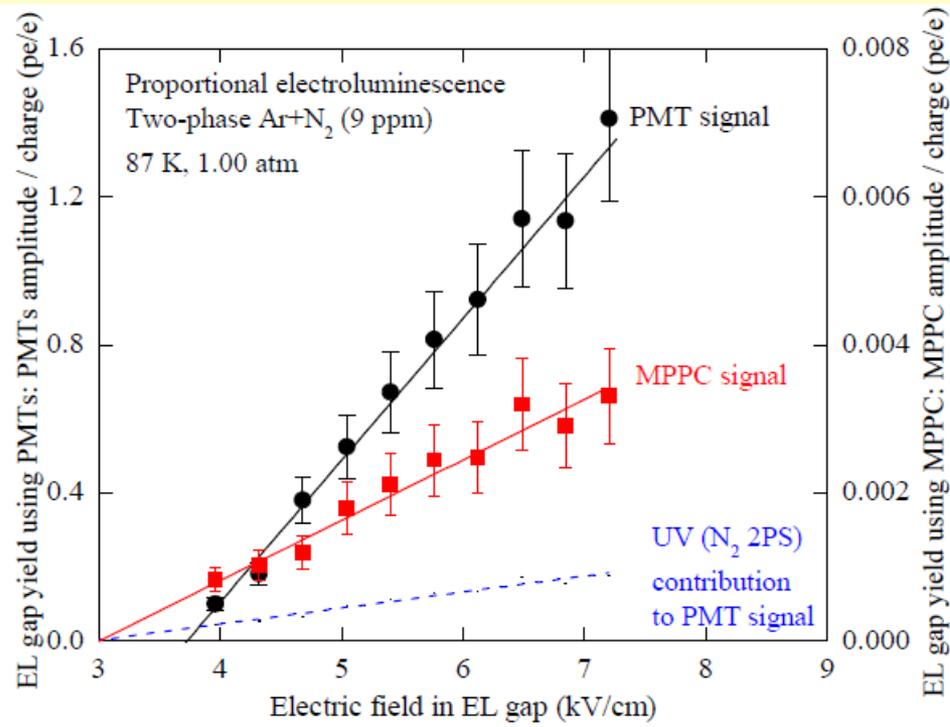
$\text{Ar}^*(3p^5 4s^1) + \text{N}_2 \rightarrow \text{Ar} + \text{N}_2^*(C)$	$k_6 \sim 1.5 \times 10^{-11} \text{ cm}^3\text{s}^{-1}$	300 K	[44,46]	
	$k_6 = 3.6 \times 10^{-11} \text{ cm}^3\text{s}^{-1}$	300 K	[59]	$2.4 \mu\text{s}$
	$k_6 \geq 6.5 \times 10^{-9} \text{ cm}^3\text{s}^{-1} (?)$	87 K	[11]	$\leq 13 \text{ ns} (?)$

A. Buzulutskov EPL 117 (2017) 39002

The problem of proportional EL in two-phase Ar

The problem of proportional EL identified in our works [EPL, 112 \(2015\) 19001](#), [EPL, 117 \(2017\) 39002](#), [J. Instrum. 12 \(2017\) C05016](#), in two-phase Ar+N₂ (10-50ppm):

- 1) observation of non-VUV component (in the UV and visible range), in addition to that of VUV, of not that small intensity;
- 2) at such small N₂ contents the appearance of the non-VUV emission could not be explained in a simple model of excitation transfer from Ar to N₂



The problem of proportional EL in two-phase Ar

In this work, we partially resolved the problem: we have studied proportional electroluminescence in pure gaseous Ar, without additives, in the two-phase mode.

Surprisingly, we again observed a non-VUV component in EL radiation. Moreover, this component was observed not only at higher electric fields, but also at lower fields, below the Ar excitation threshold.

These unexpected observations made us recall the idea of an additional EL mechanism in two-phase Ar, namely that of neutral bremsstrahlung (NBrS), that acts concurrently with the ordinary mechanism.

Section 2. Neutral bremsstrahlung (NBrS): history and theory

NBrS history

NBrS is produced by slow electrons when they are scattered on neutral atoms, at electron energies of the order of 1-10 eV [Firsov and Chibisov 1961, Kasyanov and Starostin 1965, Dalgarno and Lane 1966]. The NBrS effect was used to explain continuous emission spectra in a weakly ionized plasma.

More interesting is that back in 1970, the NBrS mechanism was proposed as an explanation for proportional electroluminescence in xenon [Butikov et al. 1970]. In the subsequent work [DeMunari and Mambriani 1971], it was stated that in Xe the EL rate agrees, in order of magnitude, with the calculated NBrS rate of light production.

However this statement was refuted in [Dias et al. 1986]: "... mechanisms based on the direct excitation of the noble gas atoms by the electrons can fully account for the secondary light production. There is no need to consider other processes like ... neutral bremsstrahlung".

Since then bremsstrahlung in connection with electroluminescence was almost forgotten. It was mentioned only once as a possible explanation of the under-threshold electroluminescence in gaseous krypton in book [Barabash and Bolozdynya 1993], later reproduced in books [Aprile et al 2006] and [Bolozdynya 2010].

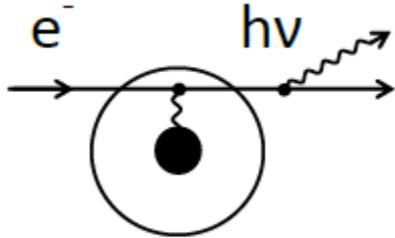
NBrS history

In the present work we show that at least for Ar the NBrS mechanism is definitely needed to explain the properties of proportional electroluminescence: we developed the theory of NBrS electroluminescence that for the first time quantitatively described the experiment at lower fields, below the excitation threshold, and that have chances to do it at higher fields, above the threshold.

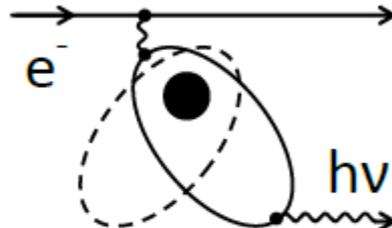
What has changed since the 70s, that has allowed us to develop a quantitative theory? → Just one thing: correct calculations of the electron energy distributions functions using Boltzmann equation solver (free software).

Accordingly, this work might be considered as a revival of the idea of NBrS electroluminescence, on a new higher level.

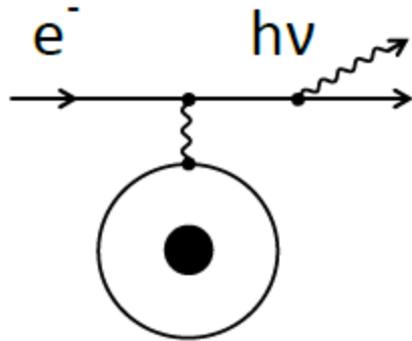
NBrS EL theory



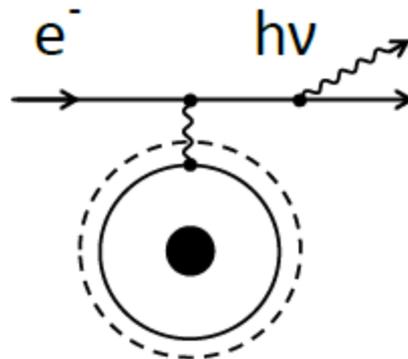
Ordinary bremsstrahlung



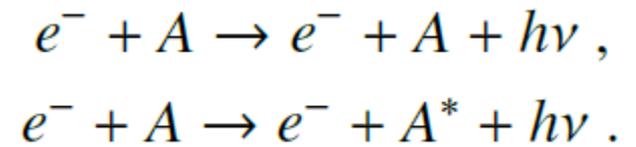
Polarization bremsstrahlung



Neutral bremsstrahlung
in elastic scattering



Neutral bremsstrahlung
in inelastic scattering



NBrS EL theory: basic equations

$$\left(\frac{d\sigma}{dv}\right)_{NBrS,el} = \frac{8}{3} \frac{r_e}{c} \frac{1}{h\nu} \left(\frac{E - h\nu}{E}\right)^{1/2} \times [(E - h\nu) \sigma_{el}(E) + E \sigma_{el}(E - h\nu)]$$

$$\frac{dI_{ph}(\lambda)}{d\lambda} = \frac{dN_{ph}}{dt N_e dV d\lambda} = N \int_{h\nu}^{\infty} v_e \frac{d\sigma}{dv} \frac{dv}{d\lambda} f(E) dE$$

in photon/(s nm electron) ,

$$\left(\frac{Y_{EL}}{N}\right)_{NBrS} = \frac{dN_{ph}}{dx N N_e dV} = \frac{1}{v_d N} \int_{\lambda_1}^{\lambda_2} \frac{dI_{ph}(\lambda)}{d\lambda} d\lambda = \int_{\lambda_1}^{\lambda_2} \int_{h\nu}^{\infty} \frac{v_e}{v_d} \frac{d\sigma}{dv} \frac{dv}{d\lambda} f(E) dE d\lambda$$

in (photon cm²)/(electron atom)

$$\frac{d(Y_{EL}/N)_{NBrS}}{d\lambda} = \int_{h\nu}^{\infty} \frac{v_e}{v_d} \frac{d\sigma}{dv} \frac{dv}{d\lambda} f(E) dE$$

in (photon cm²)/(electron atom nm) ,

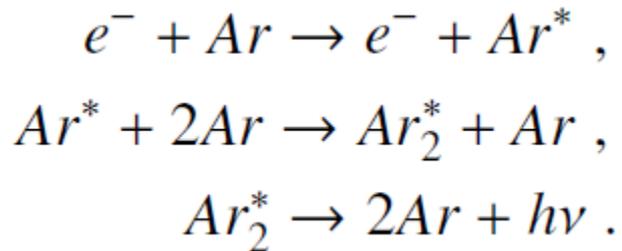
NBrS EL theory: basic equations

$$\int_0^{\infty} f(E) dE = 1$$

$$\int_0^{\infty} E^{1/2} f'(E) dE = 1$$

Electron energy distribution function normalization: two ways

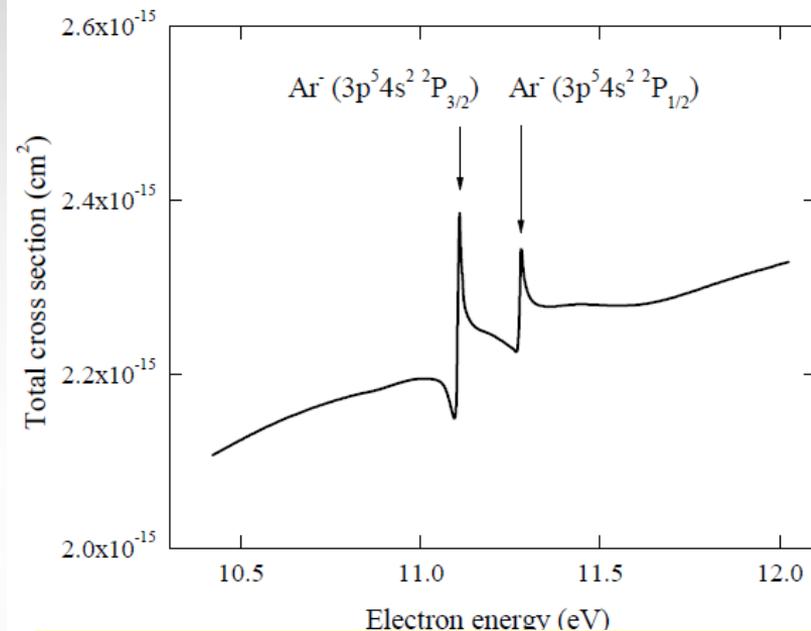
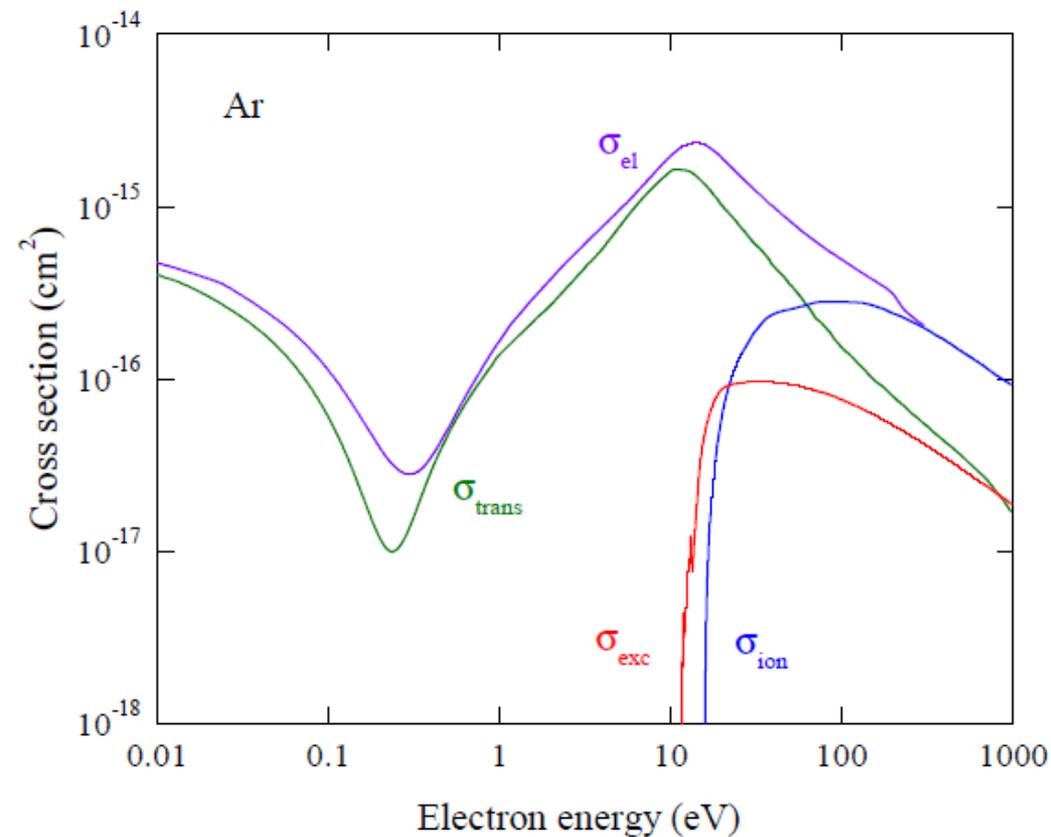
Electron energy distribution functions was calculated using Boltzmann equation solver BOLSIG+ (free software)



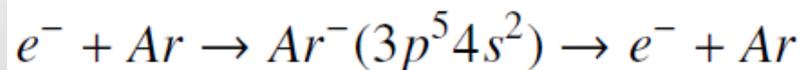
$$\left(\frac{Y_{EL}}{N}\right)_{excimer} = \int_{E_{exc}}^{\infty} \frac{v_e}{v_d} \sigma_{exc}(E) f(E) dE$$

Ordinary electroluminescence, involving excimers

NBrS EL theory: cross-sections

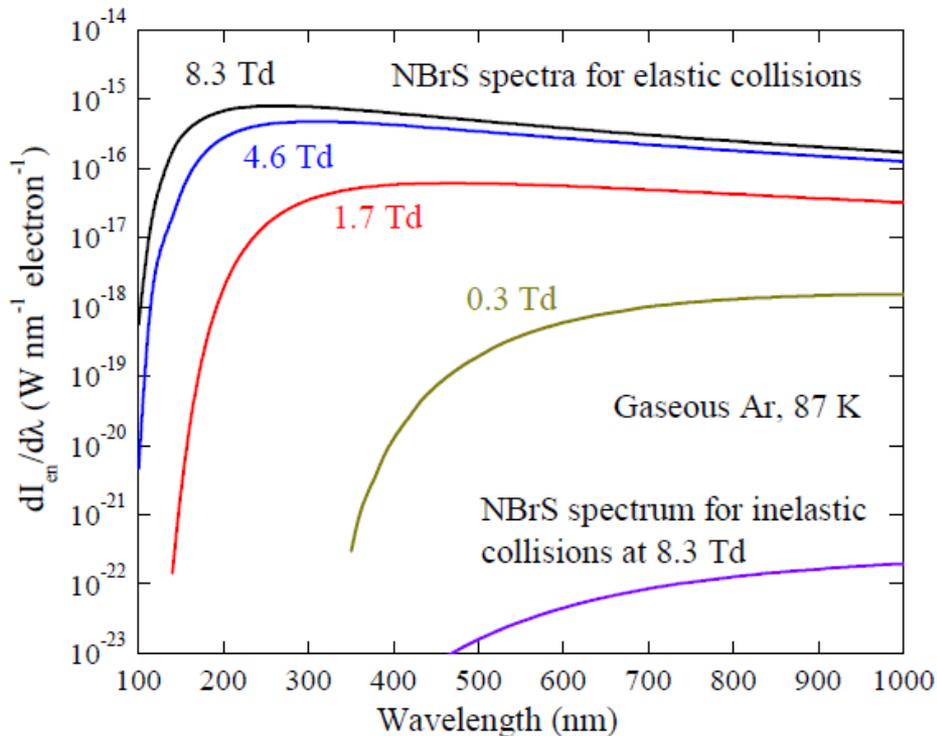


Experimental cross-section for electron scattering from Ar around Feshbach resonances [Kurokawa 2011]



Electron scattering cross-sections in Ar obtained from the last version of Magboltz

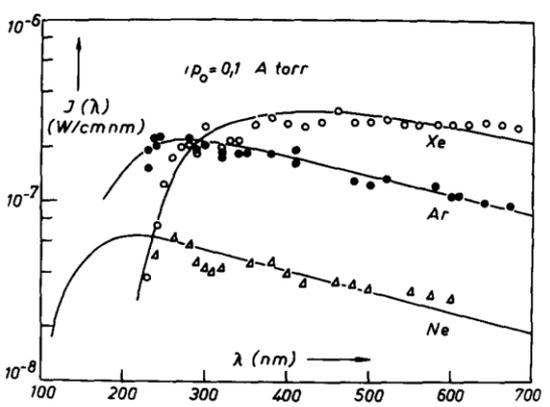
NBrS EL theory: photon emission spectra



E/N is expressed in Td.
 1 Td = $10^{-17}\ V\ cm^2\ atom^{-1}$, corresponding to $\sim 0.87\ kV/cm$ in gaseous Ar at 87 K.

NBrS spectra are rather flat.

Inelastic collision contribution can be neglected



← Comparison with NBrS spectra in glow discharge: Physica 81C (1976) 395

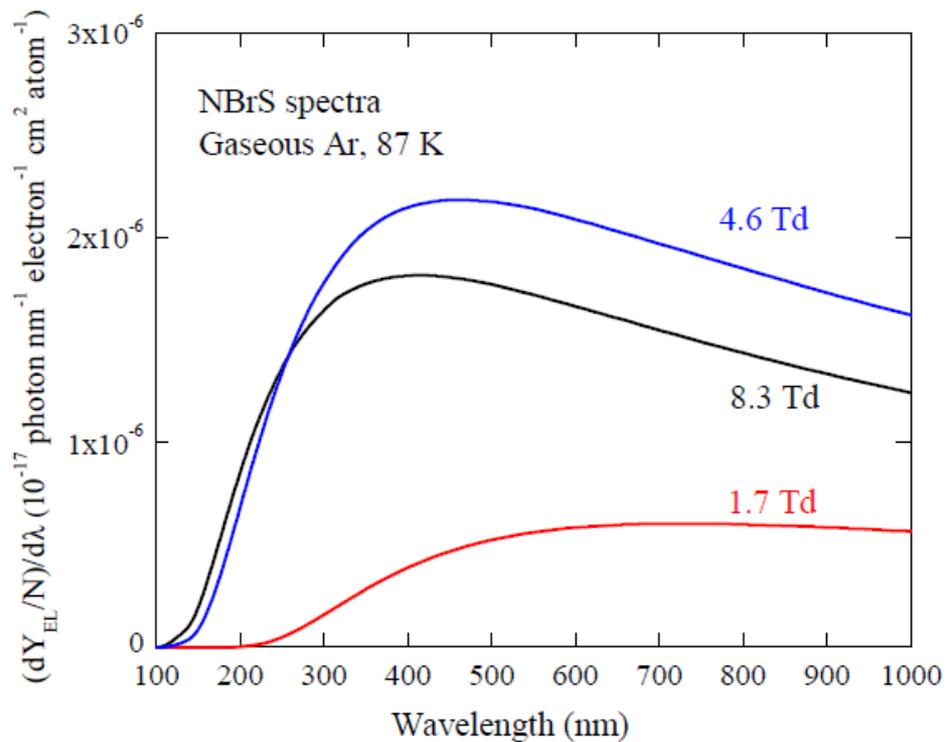
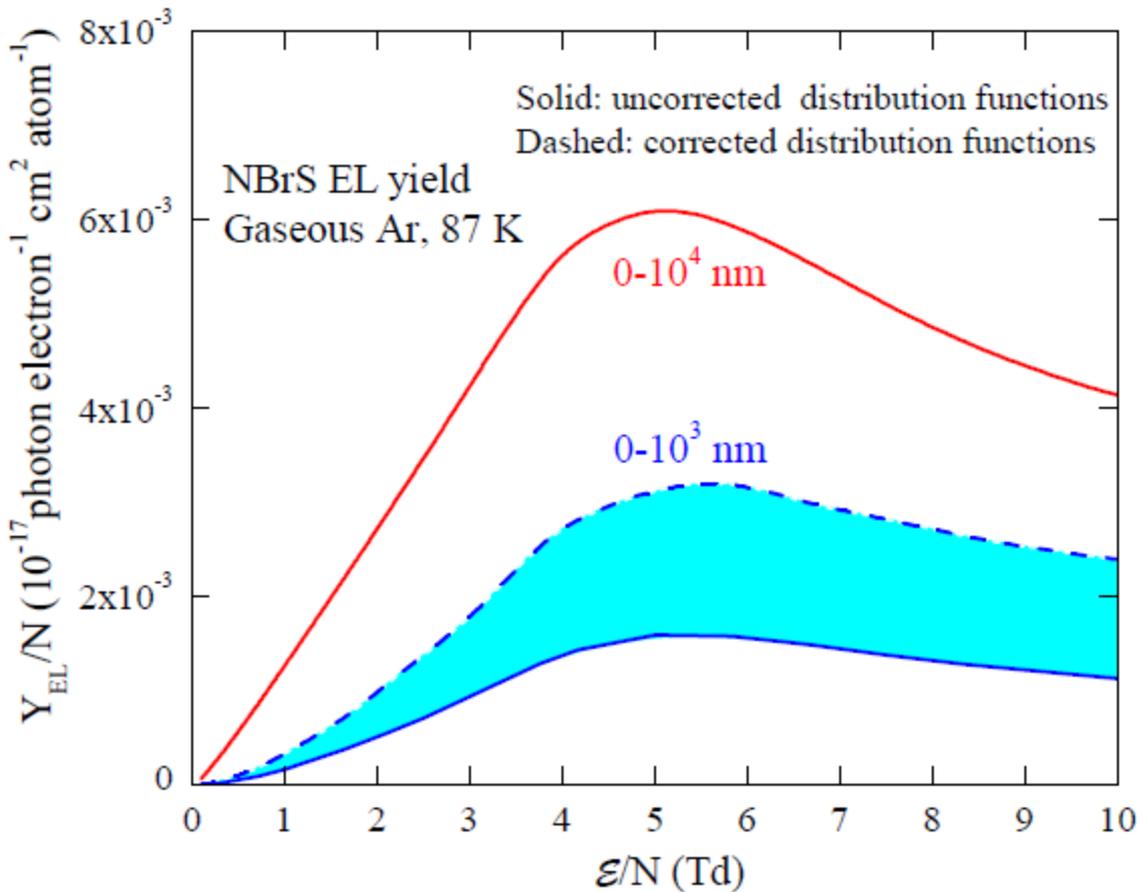


Fig. 6. Spectral intensity distributions of the continuum in Ne, Ar and Xe.

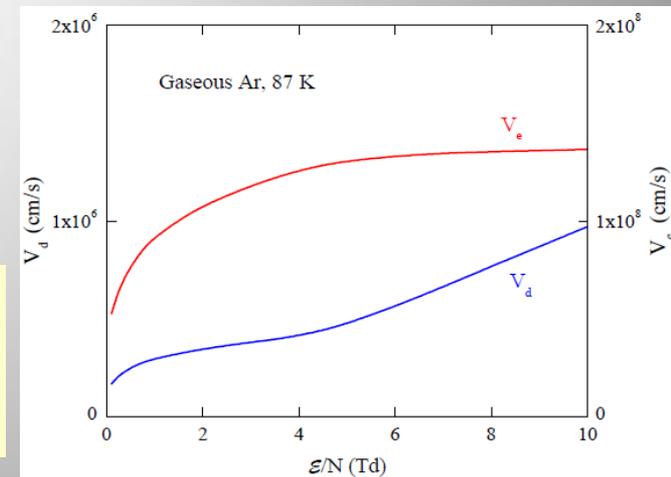
NBrS EL theory: EL yield field dependence



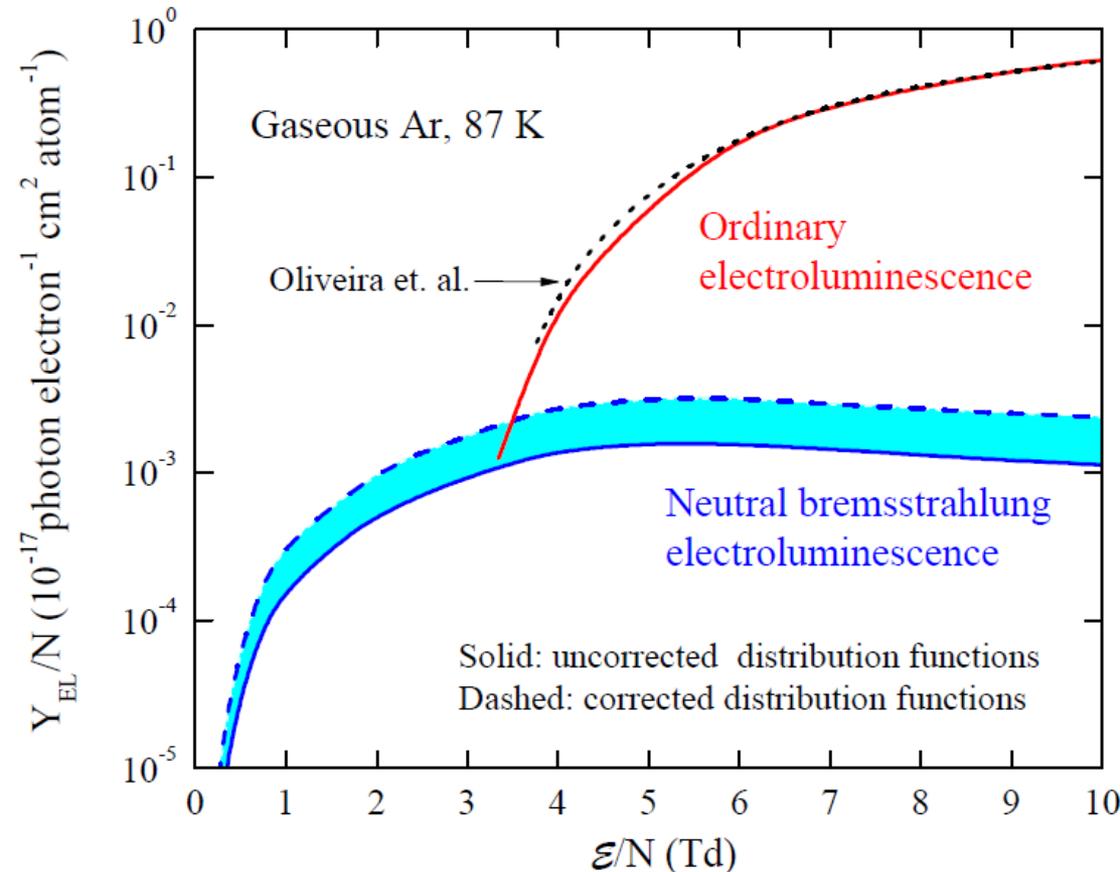
Baseline theoretical scenario

NBrS EL yield in the 0-1000 nm range represents the maximum number of NBrS photons that can ever be detected by existing devices.

NBrS EL yield first increases, then saturates and even decreases with the field: this reflects v_e/v_d behavior →



EL yield theory: NBrS EL vs ordinary EL



Baseline theoretical scenario
(without effects of Feshbach resonances)

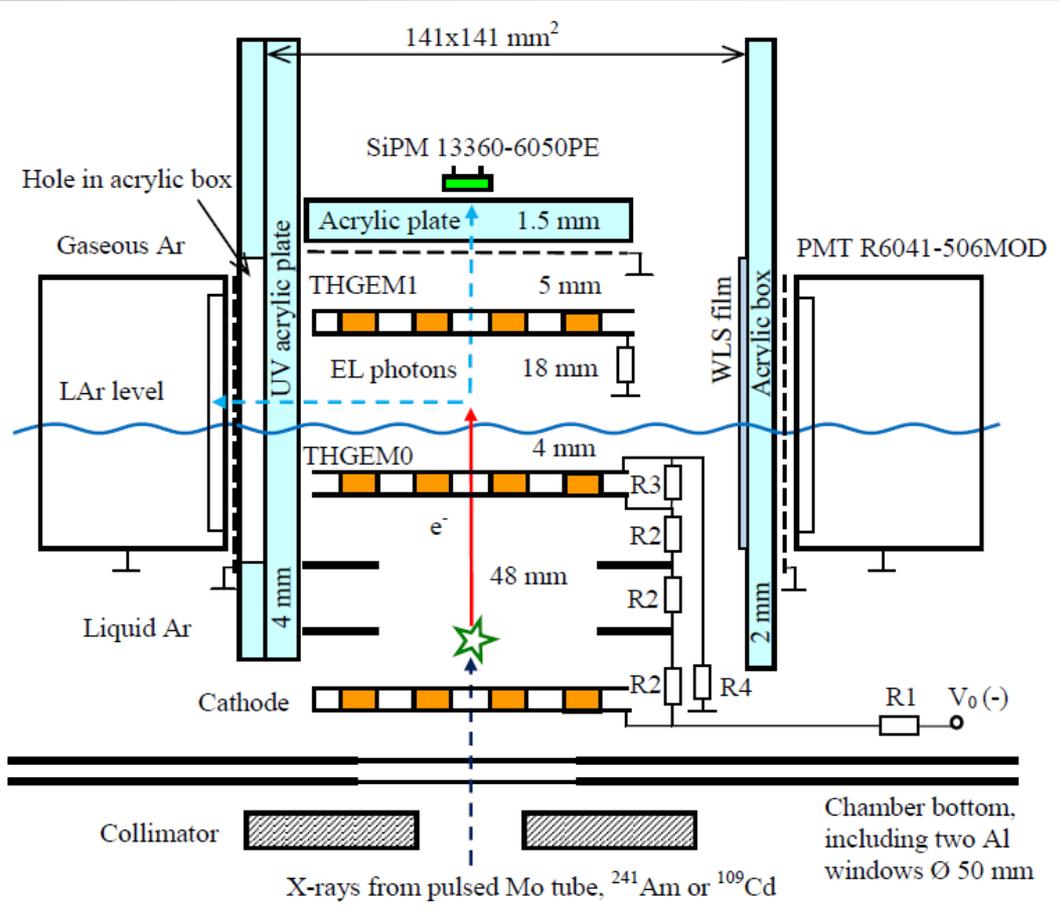
Two distinct field regions:
below and above 4 Td;
4 Td corresponds to beginning
of Ar excitation processes.

Summarizing, the theory of NBrS EL predicts:

- 1) electroluminescence below the Ar excitation threshold, in the UV, visible and NIR regions;
- 2) appreciable non-VUV component above the Ar excitation threshold, extending from the UV to NIR.

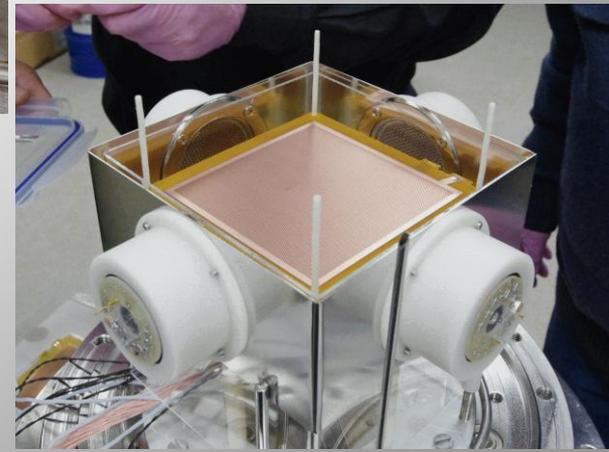
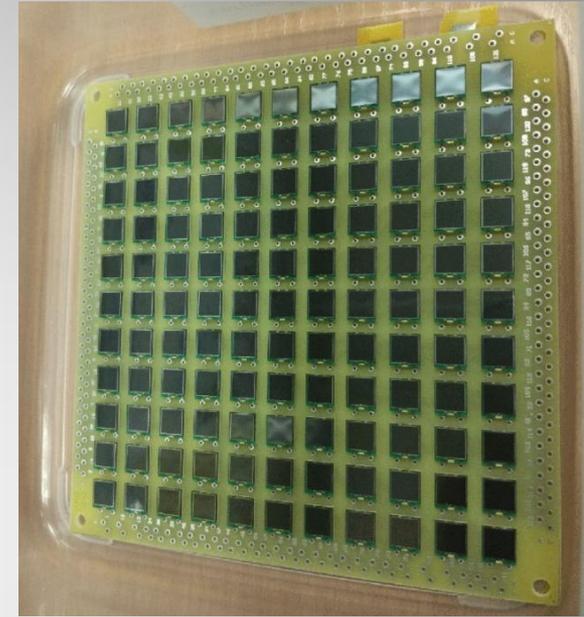
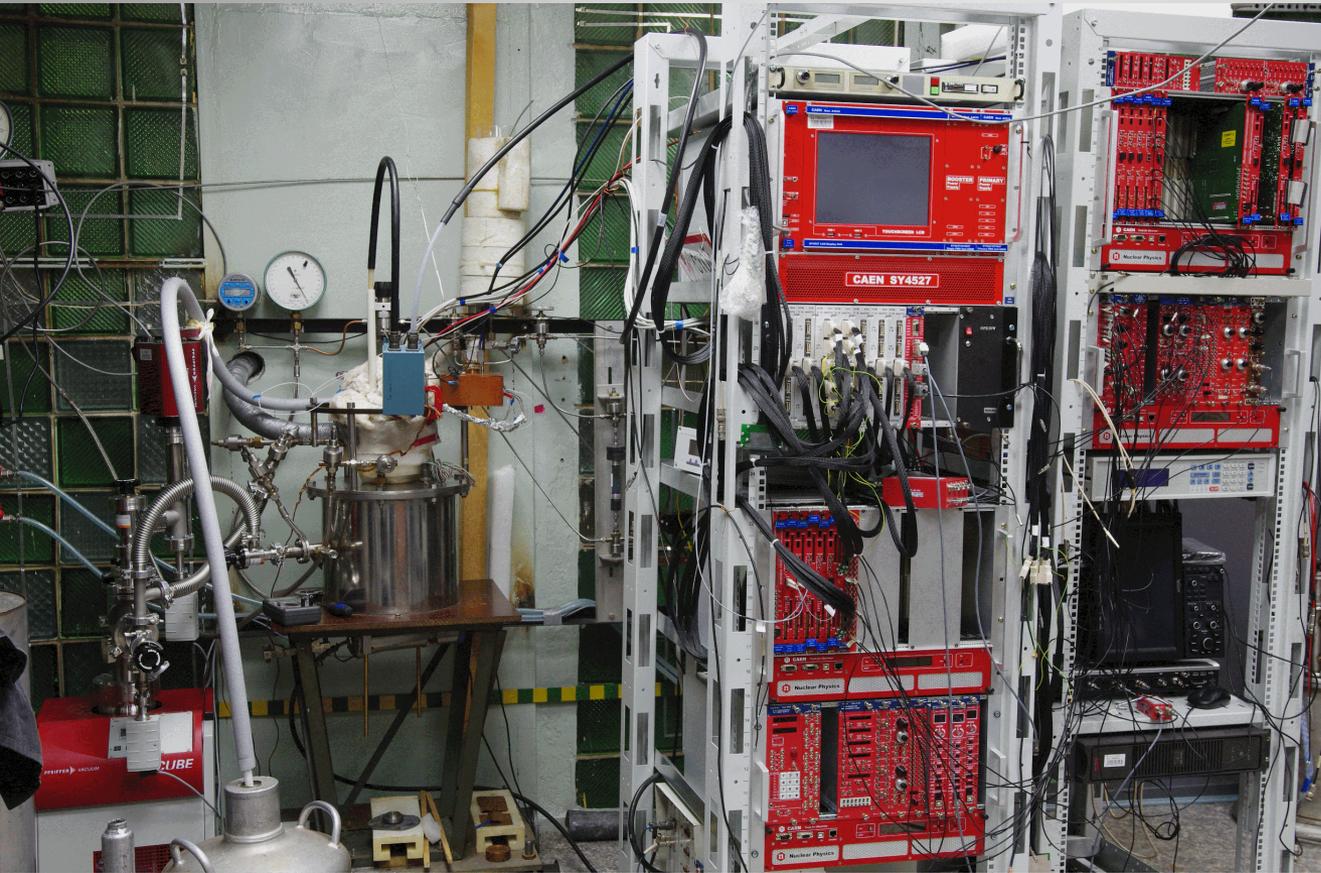
Section 3. Experimental setup

Experimental setup

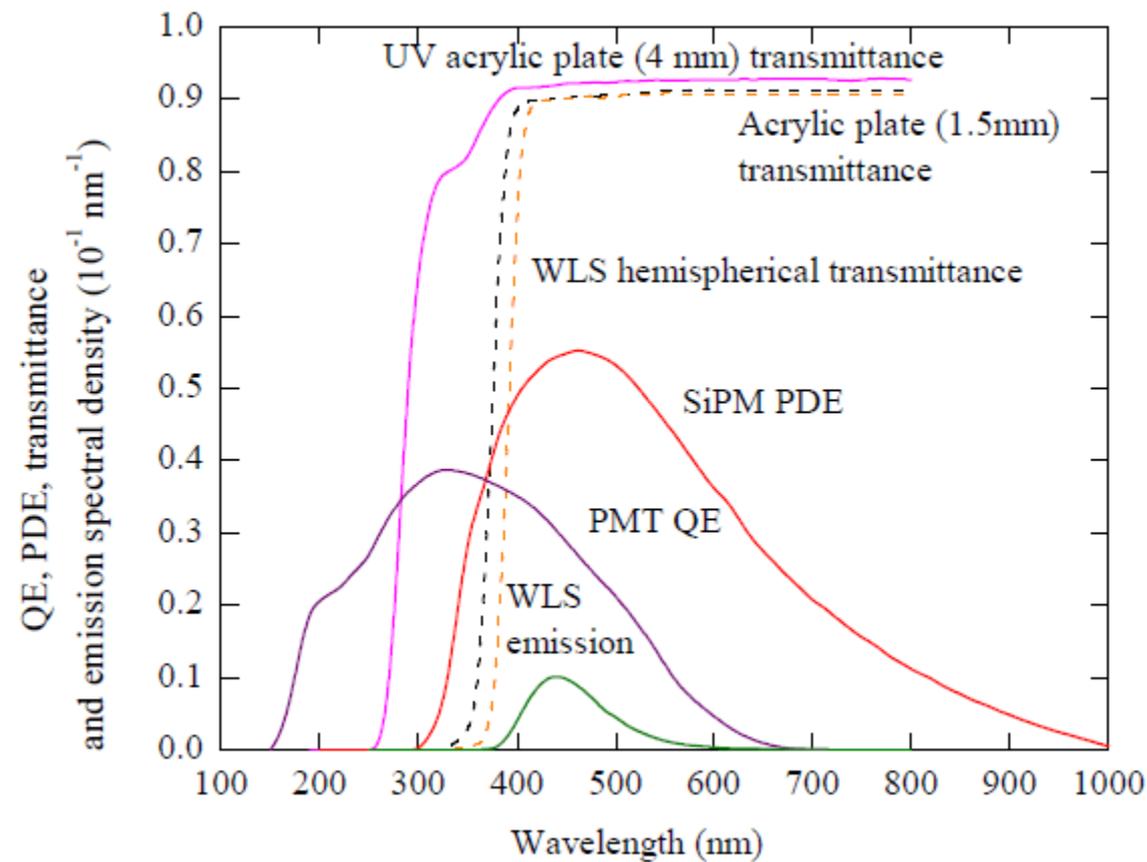


- Two-phase TPC with EL gap.
- 2.5 liters of liquid Ar.
- e- lifetime >100 us.
- O₂ <10 ppb, N₂ <1ppm.
- EL gap formed by 2 THGEMs.
- 3 ways of optical readout of S2 in EL gap: bare 1PMT, 3PMT+WLS and 5x5 SiPM-matrix.
- We had to measure WLS conversion efficiency, using S1 from vertical cosmic muons.
- DAQ system: 4-channel oscilloscope LeCroy WR HRO 66Zi and 64-channel Flash ADC CAEN V1740 (12 bits, 62.5 MHz).

Experimental setup



Experimental setup

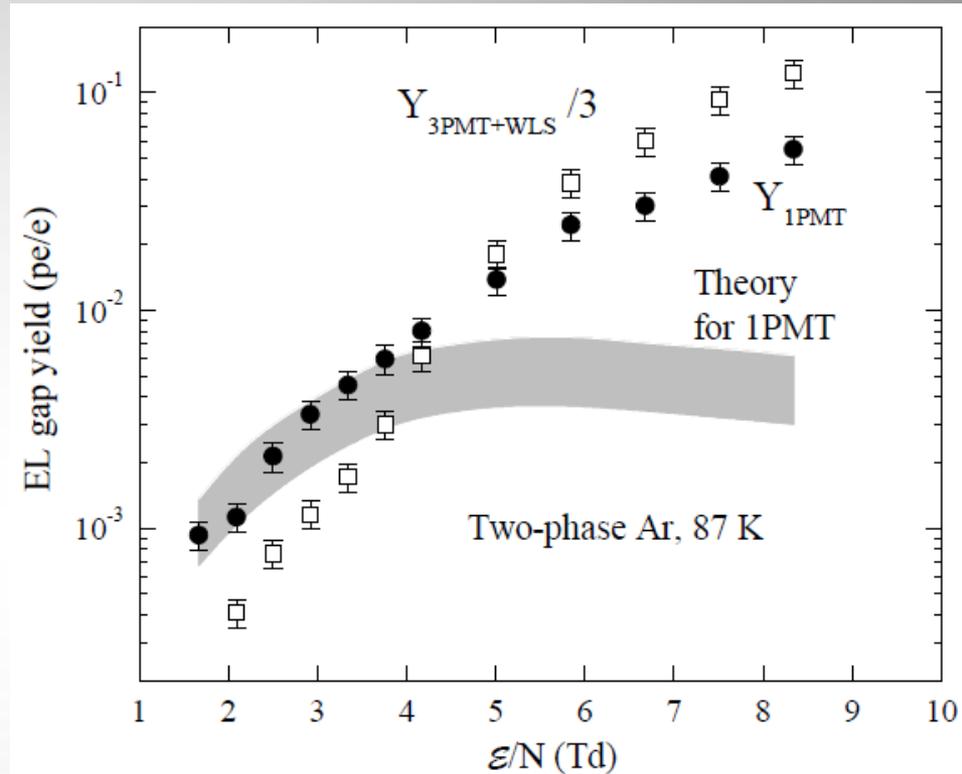
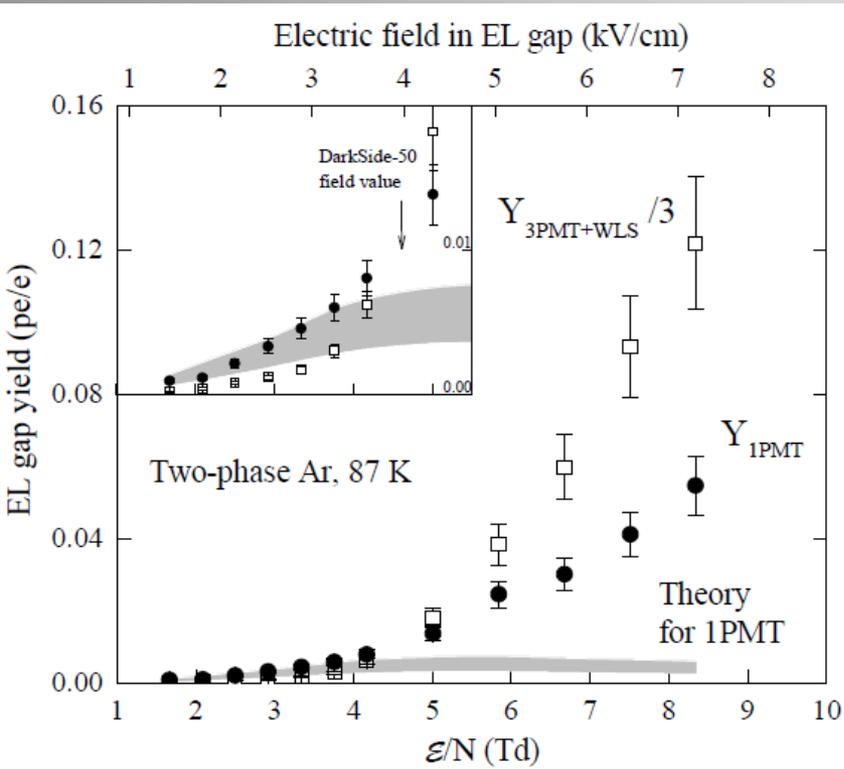


- Elaborated Monte-Carlo software for photon propagation and calculation of acceptances for the variety of readout configurations.
- Spectra convolutions.
- Accounting for SiPM PDE dependence on voltage.

- 3 types of photosensors provide 3 different spectral ranges of optical readout of S2:
- in VUV (around 128 nm), using PMT+WLS;
 - in near UV and visible (300-600 nm), using mostly bare PMT (+UV acrylic);
 - in visible and NIR (400-1000 nm), using SiPM (+acrylic).

Section 4. EL yields: experiment vs theory

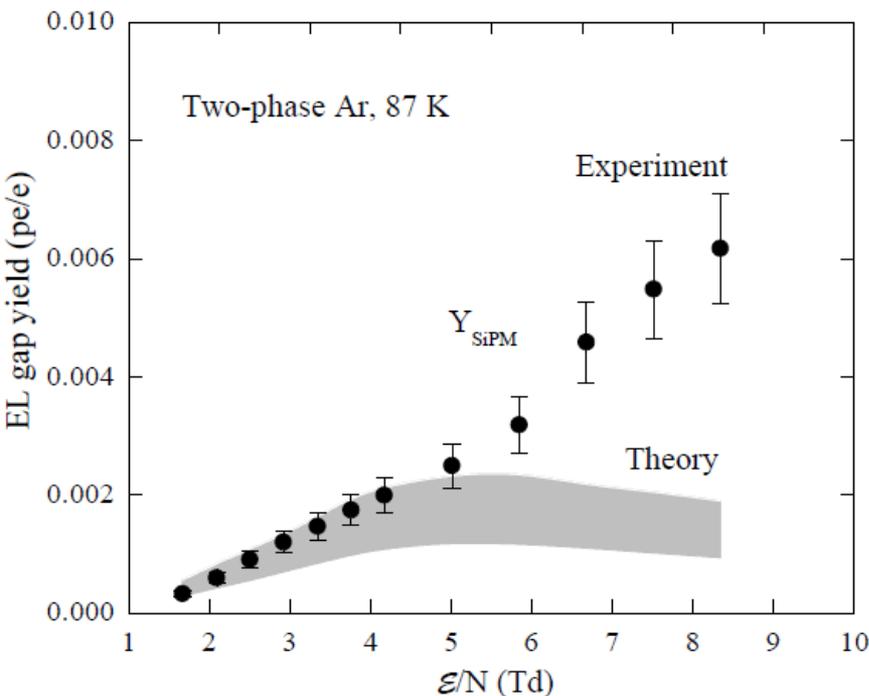
EL gap yield



$$Y_{XX} = N_{pe}/q_e ; XX=1\text{PMT}, 3\text{PMT+WLS} \text{ or SiPM}$$

- Electroluminescence below Ar excitation threshold (at 4.0 Td), where non-VUV component fully dominates.
- Substantial contribution of non-VUV component above the threshold.
- Strong response of bare PMT: as large as 40% of PMT+WLS amplitude at higher field, at 8.3 Td. At lower fields, below 4.6 Td (that of DarkSide-50), bare PMT amplitude starts exceeding that of the PMT+WLS

EL gap yield



EL gap yield for SiPM readout fully confirms the results of 1PMT readout:

- electroluminescence below the threshold;
- constantly increasing EL yield above the threshold.

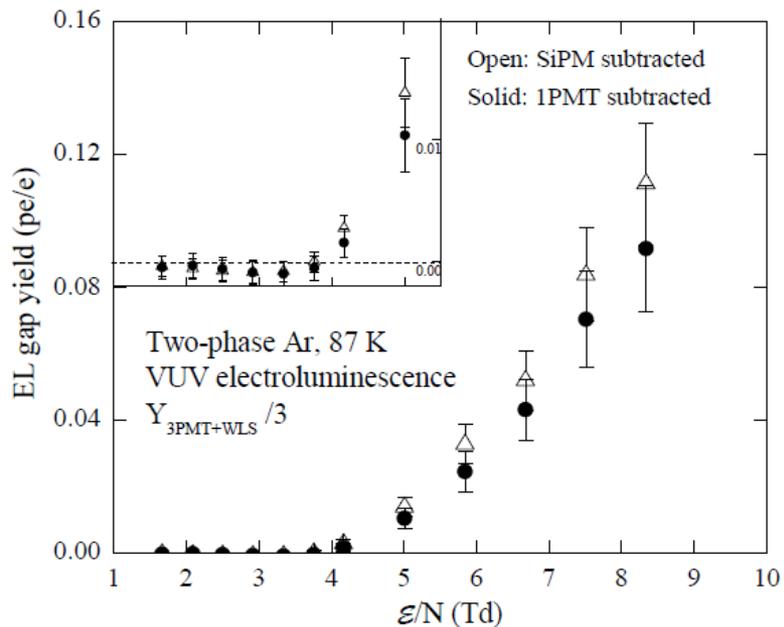
- Non-VUV component is well described by NBrS theory, below Ar excitation threshold.
- Above the threshold, the theory quickly diverges from experiment.

Back in 80s, it was suggested how to eliminate such a discrepancy:

- To account for possible electron trapping at Feshbach resonance energies, which leads to enrichment of the high-energy tail of the electron energy distribution function [De'Munari 1971, 1984].
- It was theoretically demonstrated that the NBrS yield at resonance is significantly (>3 times) enhanced [Dallacasa and Leonardis 1980].

Relying on these hypotheses, we adopt here the paradigm that all the data on non-VUV component are those induced by NBrS electroluminescence.

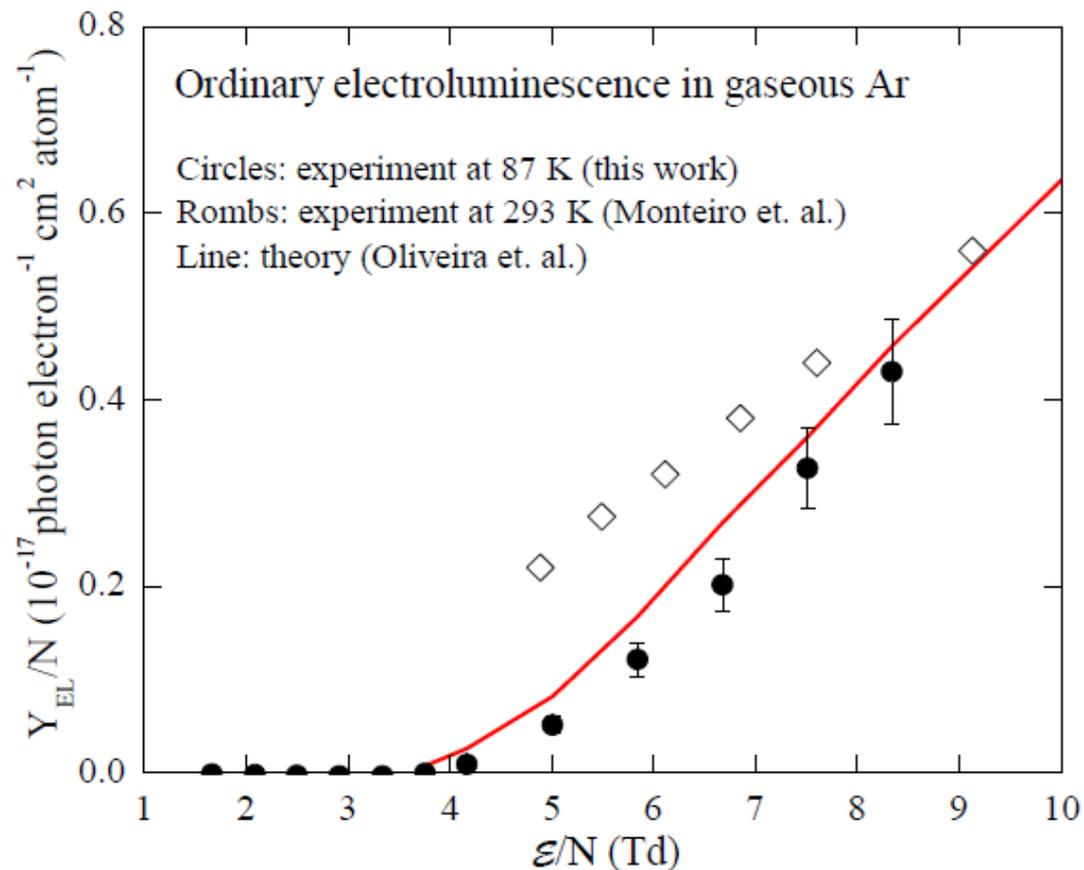
Reduced EL yield in the VUV



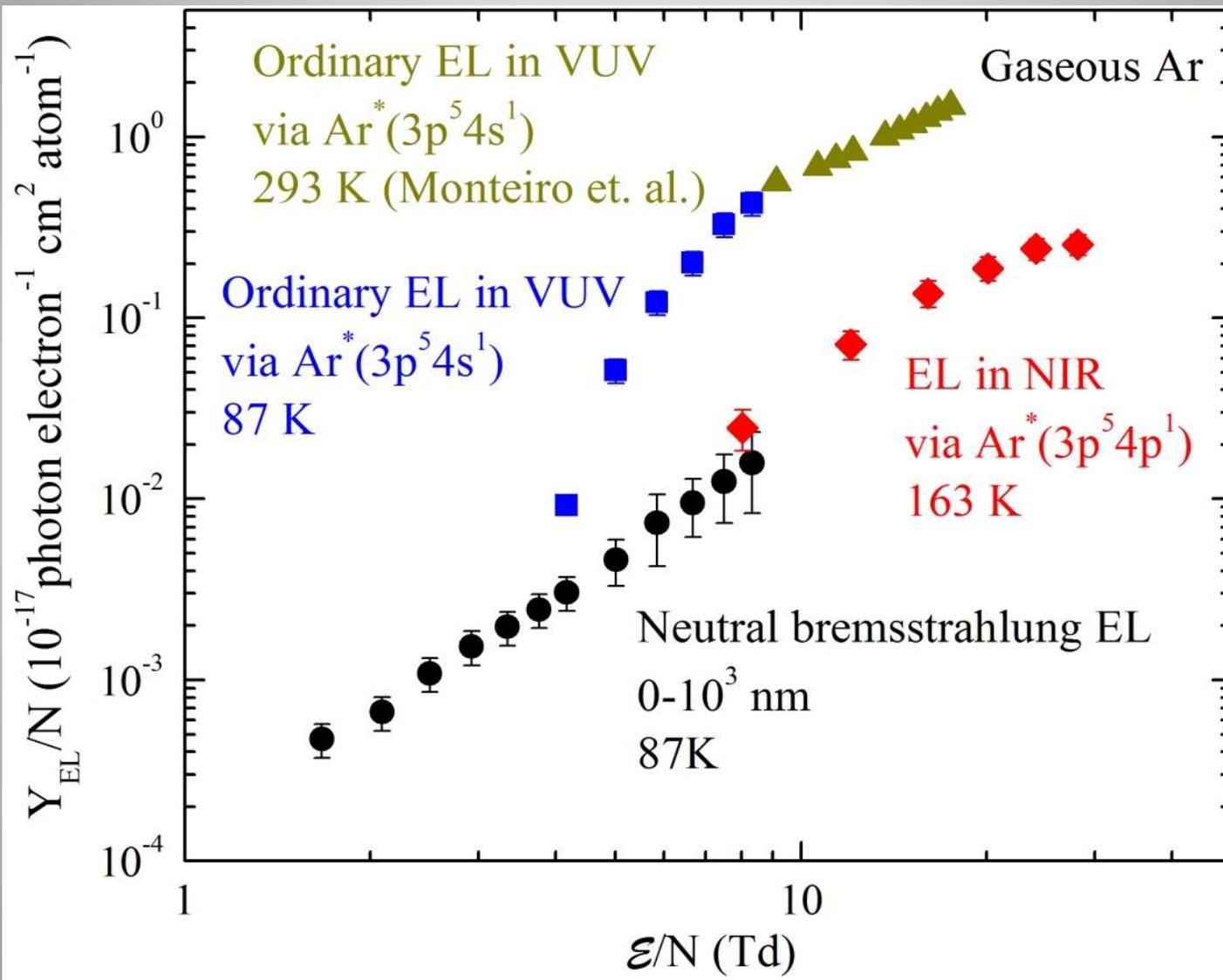
True EL gap yield for ordinary (VUV) electroluminescence from 3PMT+WLS data, where non-VUV component is subtracted using 1PMT and SiPM data, the shapes of emission spectra being provided by NBrS theory.

Reduced EL yield for ordinary (VUV) electroluminescence obtained in this work and compared to the yields at room T obtained experimentally and theoretically [Oliveira 2011].

→ Convincing agreement between the theory and our experiment, the latter using NBrS EL paradigm on non-VUV component origin.



Summary of experimental EL yield in gaseous Ar



Section 5. Applications of NBrS EL

Resolving the problem of proportional electroluminescence in two-phase Ar: the admixture of N₂ to Ar at minor contents (~50 ppm) cannot be responsible for the non-VUV component; most probably it is NBrS responsible for that.

The amplitude of the S₂ signal from the bare PMT (without WLS) is comparable with that of the PMT with WLS (in the absence of optical contact between the WLS and the PMT): paves the ways to direct PMT and SiPM-matrices optical readout of S₂.

The presence of NBrS component in proportional EL may result in suggesting to analyze the S₂ pulse-shape in a new way, in particular in two-phase Ar dark matter detectors.

Due to universal character of NBrS EL effect, it should be present in other noble gases. In particular, NBrS EL should be present in S₂ signals of two-phase Xe detectors.

NBrS electroluminescence should be present in avalanche scintillations, which are used in combined THGEM/SiPM and THGEM/CCD multipliers.

NBrS effect can be responsible for proportional electroluminescence observed in liquid Ar and Xe using immersed GEM-like structures.

It is possible that NBrS emission is present also in S₁ signals, i.e. in primary scintillations in liquid Ar, in the form of weak scintillations in the visible and NIR range observed earlier by a number of groups.

Summary

An additional mechanism of proportional electroluminescence (EL) in two-phase dark matter detectors, namely that of neutral bremsstrahlung (NBrS), has been studied. It explains the non-VUV spectral component and photon emission below the Ar excitation threshold, thus partially resolving the problem of proportional electroluminescence in two-phase Ar.

The merit of the present work is that it transformed the idea of NBrS electroluminescence from a hypothesis into a quantitative theory. This allowed to correctly determine the EL yield of proportional electroluminescence in pure gaseous Ar, at cryogenic temperature in the two-phase mode.

The main practical application of the NBrS effect is a better understanding of the S2 signal and justification for its direct (without WLS) optical readout using PMTs and SiPM-matrices, which may help to develop two-phase dark matter and neutrino detectors of ultimate sensitivity.

Backup slides

Example of two-phase detector: DarkSide-50

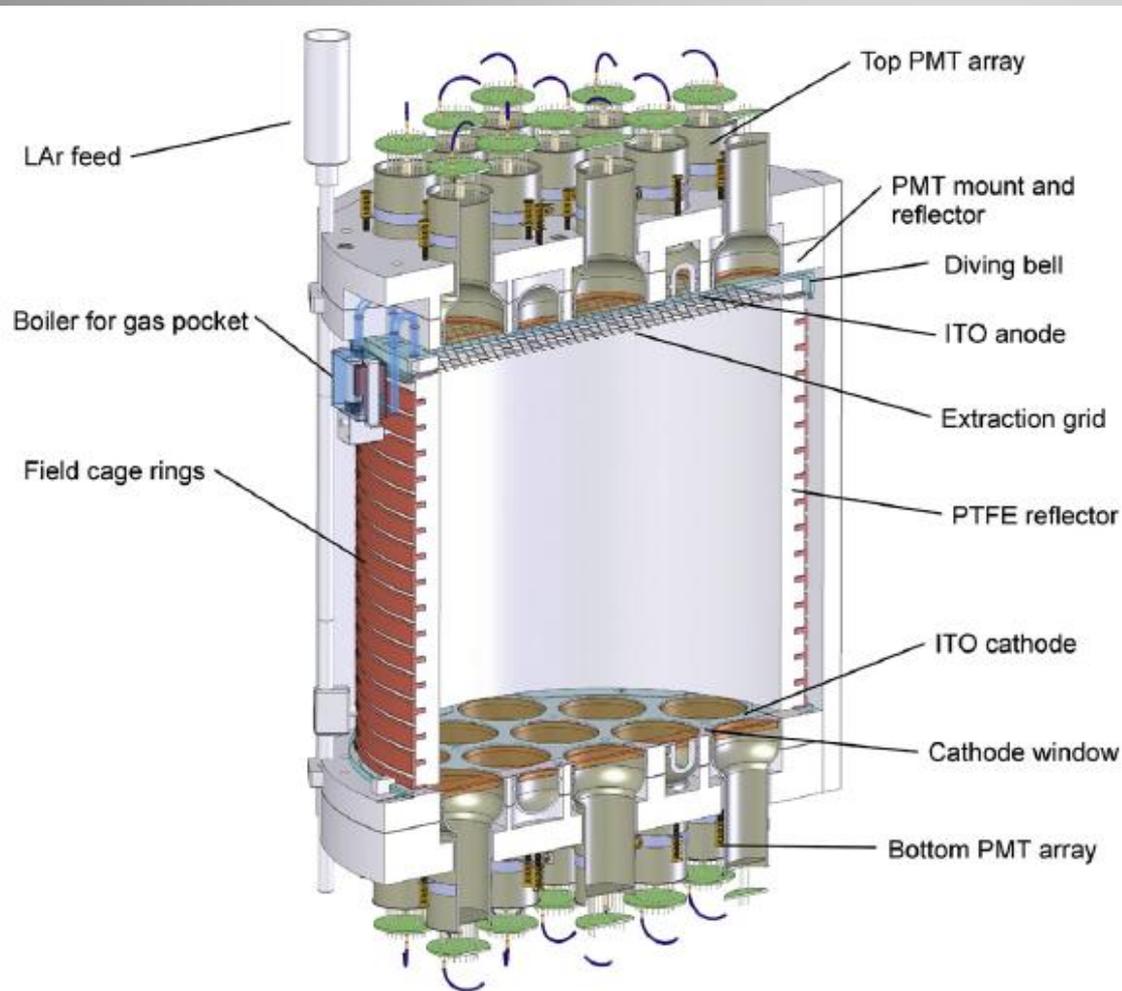


Fig. 2. The DarkSide-50 liquid argon time projection chamber.

Drift field in LAr 200 V/cm
Extraction field in LAr 2.8 kV/cm

EL gap field 4.2 kV/cm, at a pressure of 1080 mbar, corresponding to $E/N=4.6$ Td

E/N is expressed in Td
 $1 \text{ Td} = 10^{-17} \text{ V cm}^2 \text{ atom}^{-1}$,
corresponding to $\sim 0.87 \text{ kV/cm}$ in gaseous Ar at 87 K.

Photon emission and collisional processes in gaseous and liquid Ar doped with Xe and N₂

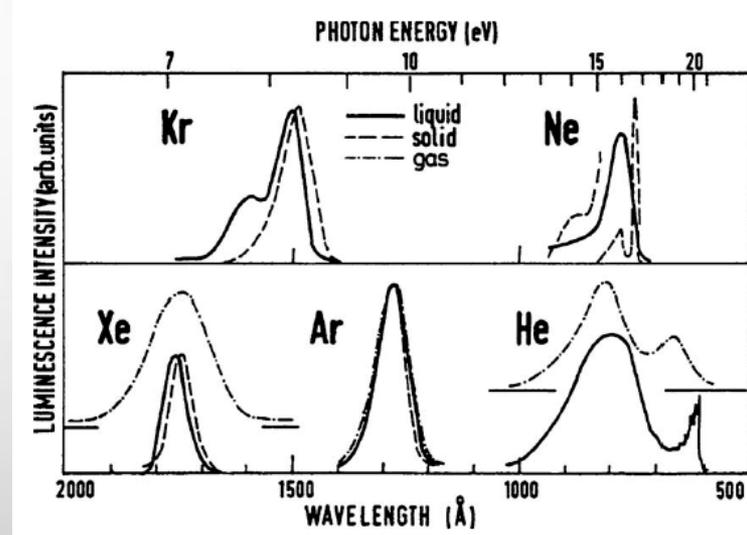
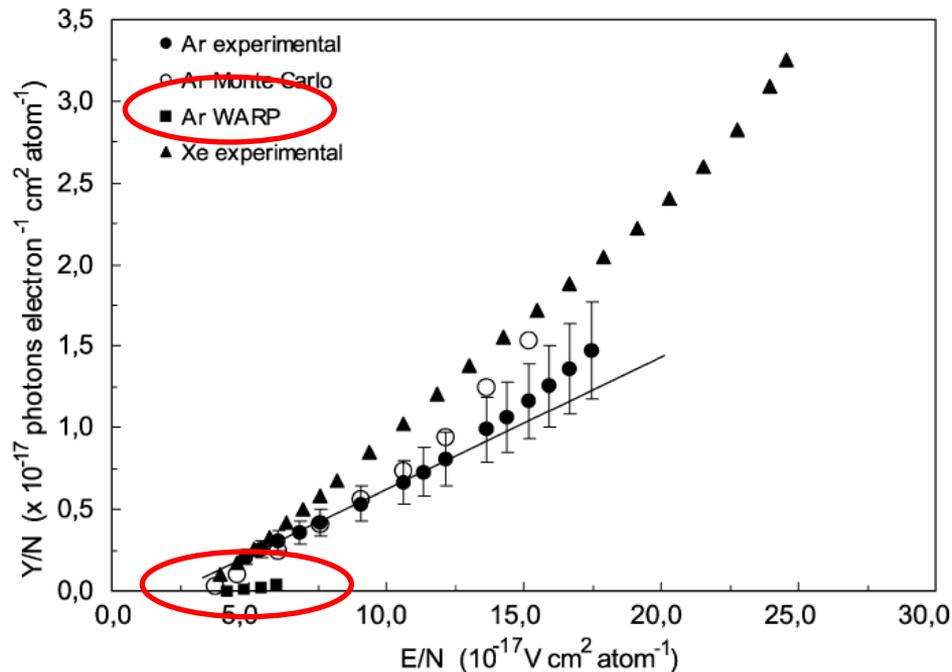
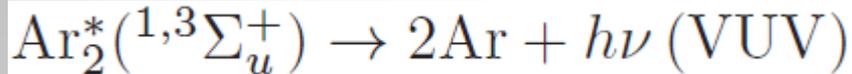
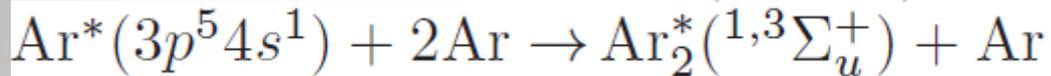
Table 1: Basic reactions of excited species relevant to the performance in the two-phase mode, namely in Ar in the gas and liquid phase, doped with Xe (1000 ppm in the liquid and 40 ppb in the gas phase) and N₂ (50 ppm in the liquid and 135 ppm in the gas phase), their rate (k) or time (τ) constants reported in the literature and their time constants reduced to given atomic densities at 87 K (τ_{TP}), in particular for Ar to that of $8.63 \times 10^{19} \text{ cm}^{-3}$ and $2.11 \times 10^{22} \text{ cm}^{-3}$ in the gas and liquid phase, respectively.

No.	Reaction	k or τ	T	Reference	τ_{TP}
<u>Gaseous Ar + Xe (40 ppb) + N₂ (135 ppm)</u>					
(1)	$\text{Ar}^*(3p^5 4s^1) + 2\text{Ar} \rightarrow \text{Ar}_2^*(^1,3\Sigma_u^+) + \text{Ar}$	$k_1 \sim 1 \times 10^{-32} \text{ cm}^6 \text{ s}^{-1}$	300 K	[44-47]	$\sim 13 \text{ ns}$
(2)	$\text{Ar}_2^*(^1,3\Sigma_u^+) \rightarrow 2\text{Ar} + h\nu \text{ (VUV)}$	$\tau_2(^1\Sigma_u^+) = 4.2 \text{ ns}$ $\tau_2(^3\Sigma_u^+) = 3.0 - 3.2 \mu\text{s}$	300 K	[48,49]	4.2 ns
(3)	$\text{Ar}^*(3p^5 4p^1) \rightarrow \text{Ar}^*(3p^5 4s^1) + h\nu \text{ (NIR)}$	$\tau_3 = 20-40 \text{ ns}$ $\tau_3 < 100 \text{ ns}$	300 K	[34,52,53]	3.1 μs
(4)	$\text{Ar}^*(3p^5 4s^1) + \text{Xe} \rightarrow \text{Ar} + \text{Xe}^*$	$k_4 = (2-3) \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$	163 K	[54-56]	$< 100 \text{ ns}$
(5)	$\text{Ar}_2^*(^3\Sigma_u^+) + \text{Xe} \rightarrow 2\text{Ar} + \text{Xe}^*(^1P_1, ^3P_1)$	$k_5 \sim 5 \times 10^{-10} \text{ cm}^3 \text{ s}^{-1}$	300 K	[13,57]	$\sim 1 \text{ ms}$
(6)	$\text{Ar}^*(3p^5 4s^1) + \text{N}_2 \rightarrow \text{Ar} + \text{N}_2^*(C)$	$k_6 \sim 1.5 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$ $k_6 = 3.6 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$ $k_6 \geq 6.5 \times 10^{-9} \text{ cm}^3 \text{ s}^{-1} \text{ (?)}$	300 K	[44,46]	2.4 μs
(7)	$\text{Ar}^*(3p^5 4s^1) + \text{N}_2 \rightarrow \text{Ar} + \text{N}_2^*(C, B, A)$	$k_7 \sim 3 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$ $k_7 = 3.6 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$	300 K	[44,46]	$\leq 13 \text{ ns} \text{ (?)}$
(8)	$\text{N}_2^*(C) \rightarrow \text{N}_2^*(B) + h\nu \text{ (UV, 2nd pos. sys.)}$	$\tau_8 = 30-40 \text{ ns}$	300 K	[44,46,60]	35 ns
(9)	$\text{N}_2^*(B) \rightarrow \text{N}_2^*(A) + h\nu \text{ (NIR, 1st pos. sys.)}$	$\tau_9 \sim 9 \mu\text{s}$	300 K	[44]	$\sim 9 \mu\text{s}$
(10)	$\text{N}_2^*(C) + \text{Ar} \rightarrow \text{N}_2^*(B) + \text{Ar}$	$k_{10} = 5.6 \times 10^{-13} \text{ cm}^3 \text{ s}^{-1}$	119 K	[38]	21 ns
(11)	$\text{N}_2^*(B) + \text{Ar} \rightarrow \text{N}_2^*(A) + \text{Ar}$	$k_{11} = 1.4 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$	300 K	[44]	0.8 μs
(12)	$\text{N}_2^*(C) + \text{N}_2 \rightarrow \text{N}_2 + \text{N}_2^*(B)$	$k_{12} \sim 1 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$	300 K	[44,60]	$\sim 8.6 \mu\text{s}$
(13)	$\text{N}_2^*(B) + \text{N}_2 \rightarrow \text{N}_2 + \text{N}_2^*(A)$	$k_{13} \sim 1 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$	300 K	[44]	$\sim 8.6 \mu\text{s}$
(14)	$\text{Ar}_2^*(^3\Sigma_u^+) + \text{N}_2 \rightarrow 2\text{Ar} + \text{N}_2^*(B)$	$k_{14} \sim 3.3 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$	300 K	[44,58]	$\sim 26 \mu\text{s}$
<u>Liquid Ar + Xe (1000 ppm) + N₂ (50 ppm)</u>					
(15)	$\text{Ar}^*(n = 1, 2, ^2P_{1/2,3/2}) + \text{Ar} \rightarrow \text{Ar}_2^*(^1,3\Sigma_u^+)$	$\tau_{15} = 6 \text{ ps}$	87 K	[25,61]	6 ps
(16)	$\text{Ar}_2^*(^1,3\Sigma_u^+) \rightarrow 2\text{Ar} + h\nu \text{ (VUV)}$	$\tau_{16}(^1\Sigma_u^+) = 7 \text{ ns}$ $\tau_{16}(^3\Sigma_u^+) = 1.6 \mu\text{s}$	87 K	[8-10,62]	7 ns 1.6 μs
(17)	$\text{Ar}_2^*(^1,3\Sigma_u^+) + \text{Xe} \rightarrow 2\text{Ar} + \text{Xe}^*(n = 1, 2, ^2P_{3/2})$	$k_{17}(^3\Sigma_u^+) \sim (0.8 - 1) \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$ $\tau_{17}(^3\Sigma_u^+) < 90 \text{ ns}$	87 K	[17-19]	$\sim 5.3 \text{ ns}$
(18)	$\text{Xe}^*(n = 1, 2, ^2P_{3/2}) + \text{Ar} \rightarrow \text{ArXe}^*$	$k_{17}(^1\Sigma_u^+) \sim 3.3 \times 10^{-11} \text{ cm}^3 \text{ s}^{-1}$	87 K	[18,20]	$< 90 \text{ ns}$
(19)	$\text{ArXe}^* + \text{Xe} \rightarrow \text{Ar} + \text{Xe}_2^*(^1,3\Sigma_u^+)$	Immediate trapping	87 K	[19]	$\sim 1.4 \text{ ns}$
(20)	$\text{Xe}^*(n = 1, 2, ^2P_{3/2}) + \text{Xe} \rightarrow \text{Xe}_2^*(^1,3\Sigma_u^+)$	$\tau_{19} \leq 20 \text{ ns}$	87 K	[20]	$\leq 20 \text{ ns}$
(21)	$\text{Xe}_2^*(^1,3\Sigma_u^+) \rightarrow 2\text{Xe} + h\nu \text{ (UV)}$	$\tau_{21}(^1\Sigma_u^+) = 4.3 \text{ ns}$ $\tau_{21}(^3\Sigma_u^+) = 22 \text{ ns}$	87 K	[16]	4.3 ns 22 ns
(22)	$\text{Xe}^*(n = 2, ^2P_{3/2}) \rightarrow \text{Xe}^*(n = 1, ^2P_{3/2}) + h\nu \text{ (NIR)}$	$\tau_{22} < 170 \text{ ns}$	165 K	[9,62]	4.3 ns
Reactions (17)–(21) in total ($\tau_{17} + \tau_{19}$):					$\leq 110 \text{ ns}$
(23)	$\text{Ar}_2^*(^3\Sigma_u^+) + \text{N}_2 \rightarrow 2\text{Ar} + \text{N}_2^*(B)$	$k_{23} = 3.8 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$	165 K	[21,22]	$< 170 \text{ ns}$
(24)	$\text{ArXe}^* + \text{N}_2 \rightarrow \text{Ar} + \text{Xe} + \text{N}_2^*(B, A)$	–	87 K		
(25)	$\text{Xe}_2^*(^3\Sigma_u^+) + \text{N}_2 \rightarrow 2\text{Xe} + \text{N}_2^*(B, A)$	–	87 K		

All that was known about proportional electroluminescence before the present study was reflected in [A.Buzulutskov EPL 117 (2017) 39002]

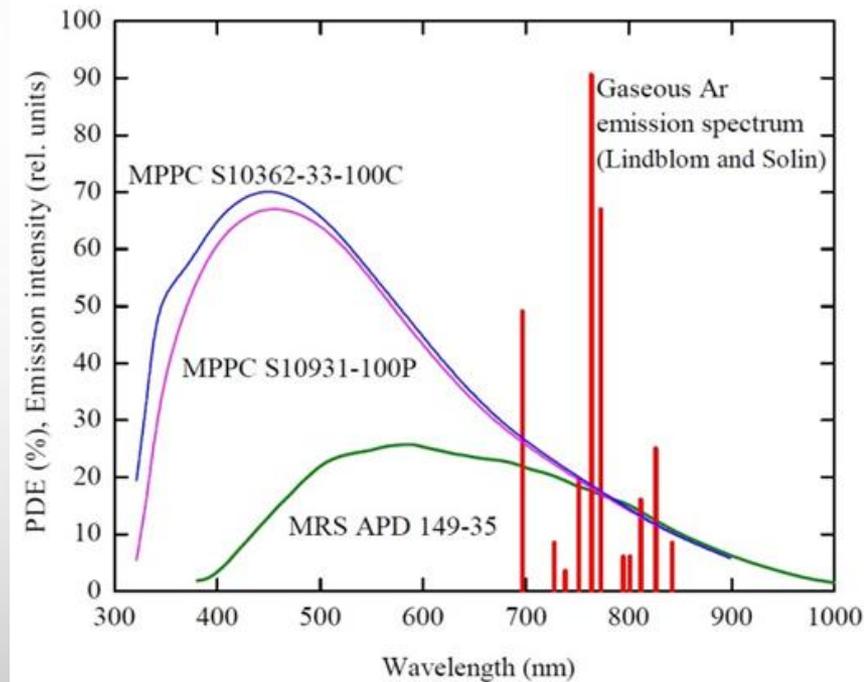
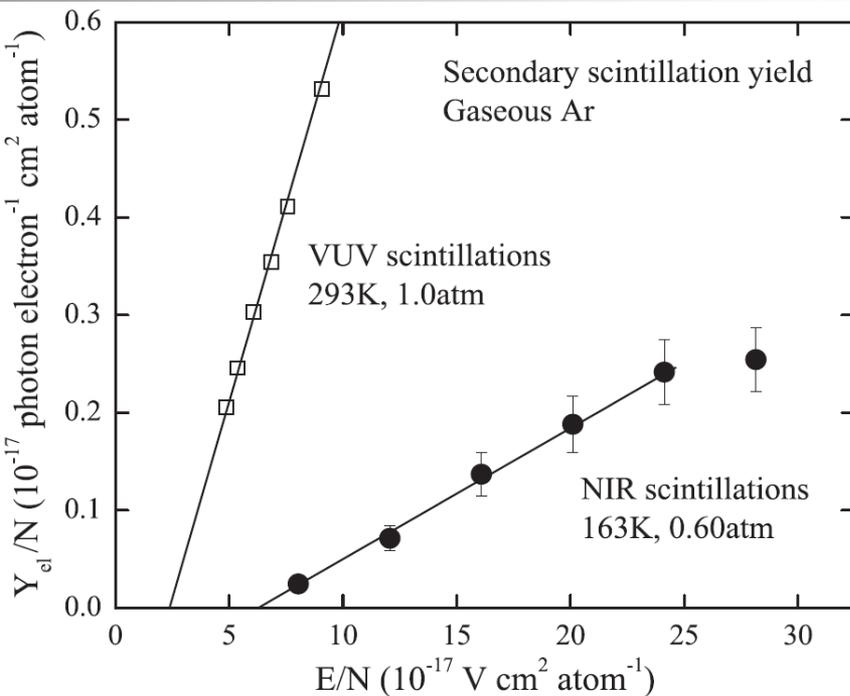
Proportional EL in GAr: ordinary EL - strong emission in VUV

Strong ordinary EL in the VUV (128 nm) due to excimers, via $\text{Ar}^*(3p^5 4s^1)$ excited states, at >4 Td:

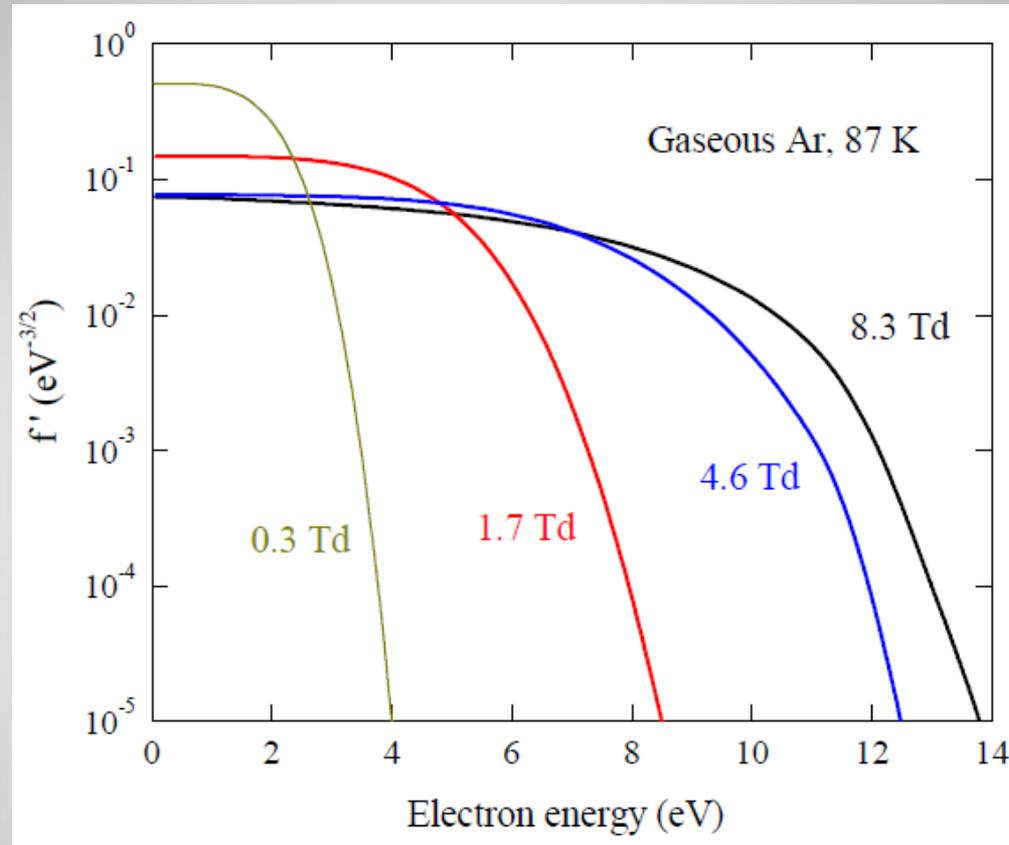


Proportional EL in GAr: additional EL - weak emission in NIR at higher fields

Weak EL in the NIR via $\text{Ar}^*(3p^5 4p^1)$ excited states, at higher electric fields, at >6 Td



NBrS EL theory: electron energy distribution functions

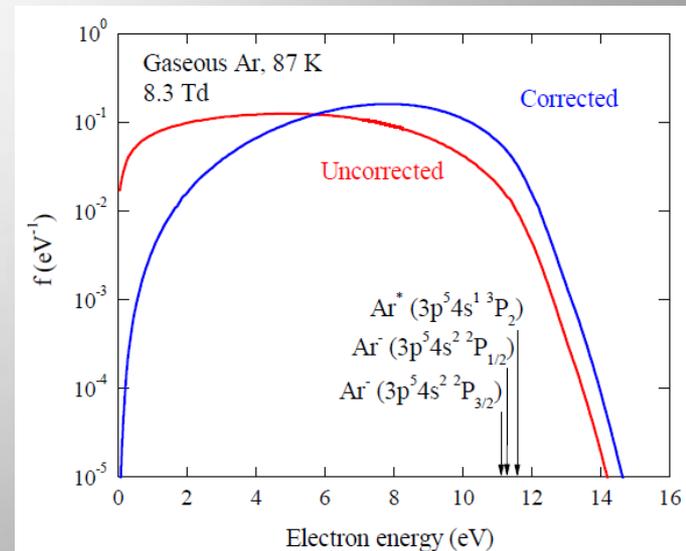
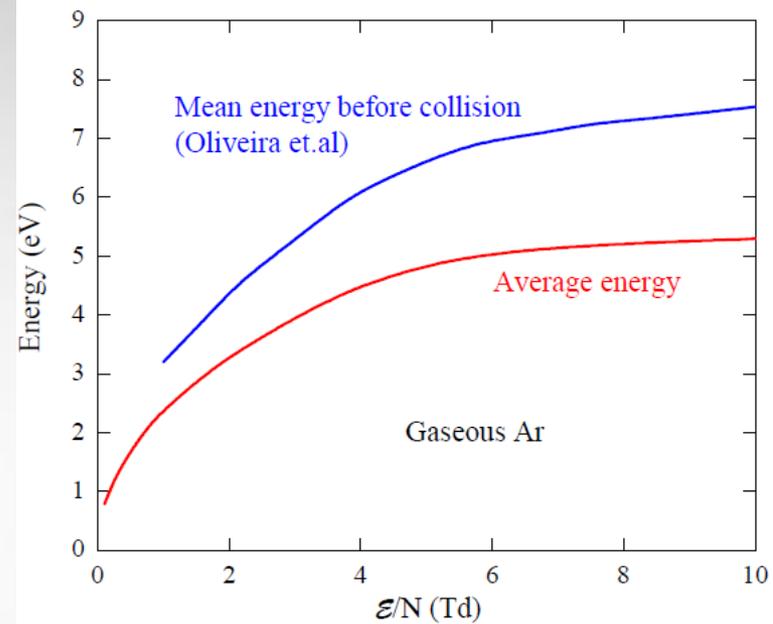
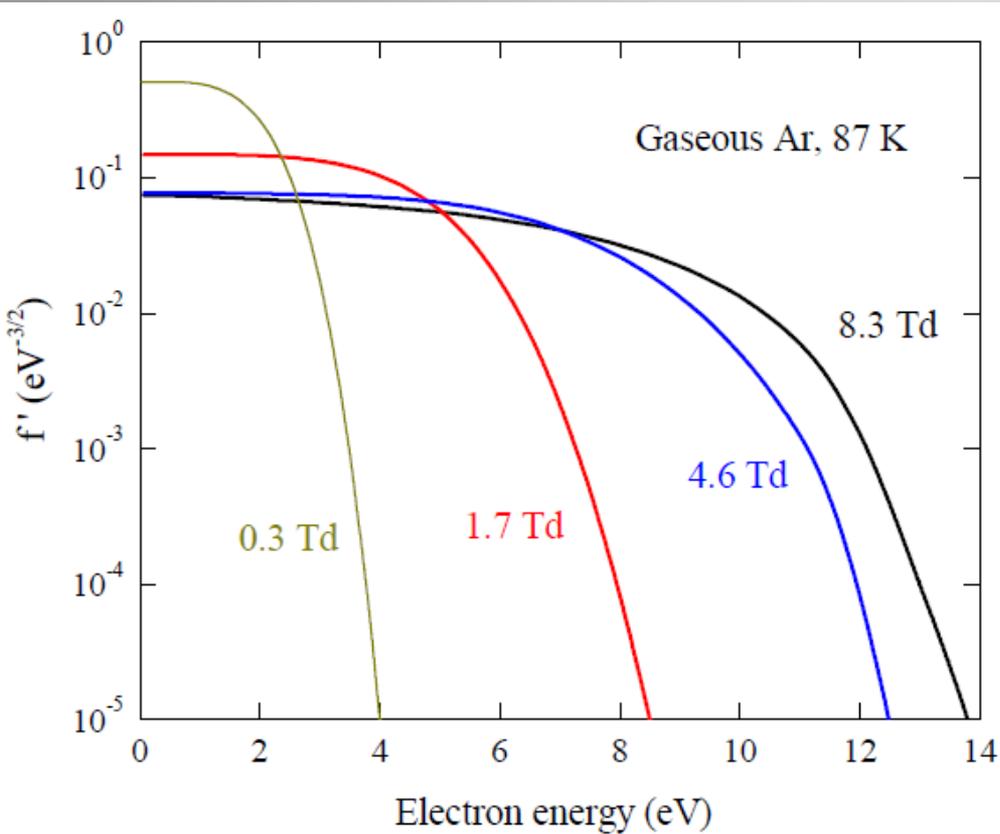


Electron energy distribution functions, calculated using Boltzmann equation solver BOLSIG+ (free software)

E/N is expressed in Td.

1 Td = 10^{-17} V cm² atom⁻¹, corresponding to ~0.87 kV/cm in gaseous Ar at 87 K.

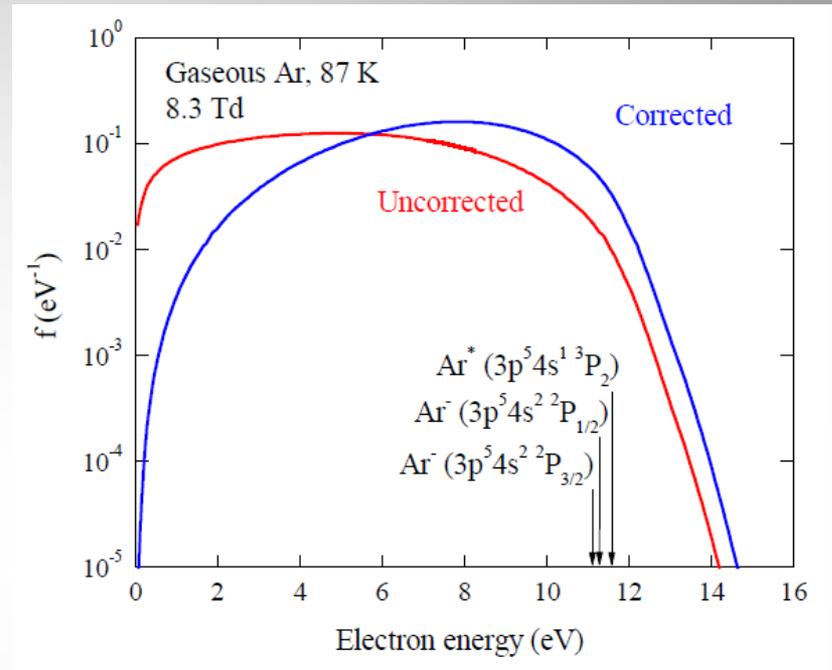
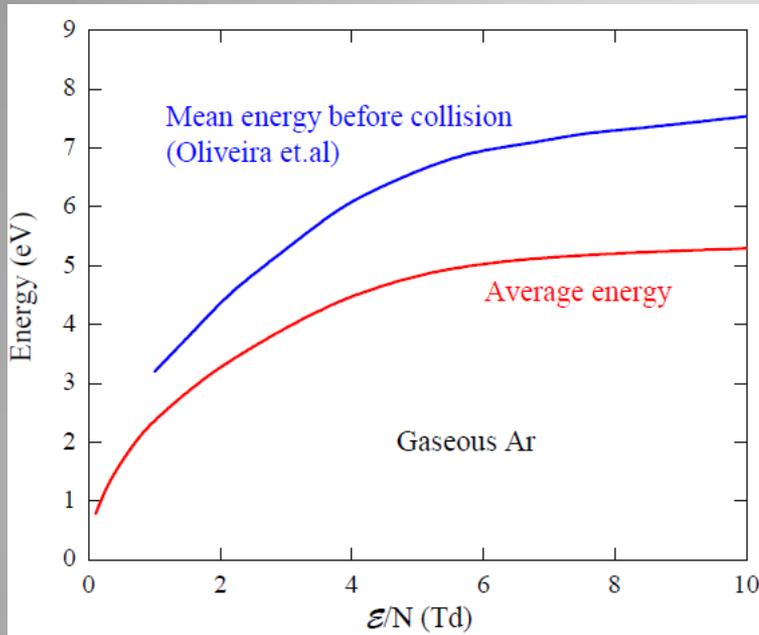
NBrS EL theory: electron energy distribution functions



Electron energy distribution functions, calculated using Boltzmann equation solver BOLSIG+ (free software)

E/N is expressed in Td.
 $1 \text{ Td} = 10^{-17} \text{ V cm}^2 \text{ atom}^{-1}$, corresponding to $\sim 0.87 \text{ kV/cm}$ in gaseous Ar at 87 K.

NBrS EL theory: uncorrected and corrected electron energy distribution functions



Electron energy distribution functions: correction for mean energy before collisions.

→ Defines the limits of theoretical uncertainty (factor of 2).

Summary of experimental EL yield in gaseous Ar

